Game Theory and the Infinity Laplacian

1. Introduction to game theory.
2. Mean Value Formula and Dynamic Programming Principle.
3. Viscosity solutions of the normalized infinity Laplacian.

Optimization Equations, Transport, and Monge-Ampère

4. Monge's problem of *déblais-remblais*. Connection with Monge-Ampère equations.
5. Kantorovich's approach: Optimal plan vs. optimal map.
6. Applications to construction of antennas and reflectors.

References

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