Collected Works / Unfolding

FLOW

In the table below, the serial numbers of A works are in black boldface, like 6 in the 1957 box (upright for mathematical papers) or like 10 for the 1966 box (italic for general papers; biographical items, like 14 in 1976, are displayed as 14). Joint papers with main collaborators are distinguished with the name and a colour code: Hirzebruch, Singer, Bott, Segal and Hitchin (Hodge, 1954 and 1955, has been displayed in superscript). Collaborations reduced to a single paper, like 26 with TODD (1960), are distinguished like 26^{To}, where the superscript code is explained at the bottom of the table. A case like 39^{Sh} (1964) means that 39 is a paper with Bott and Sh=Shapiro, and that the latter appears only once in CW. The colour of superscripts D, G, M and Su (Donelly, Gårding, Manton, Sutcliffe) indicates that they appear twice, and P (PATODI), that he appears four times (he may be ranked as one of the main collaborators). Finally, ||, ||, || and // mean transition to CW 2, 3, 4, 5 and 6, respectively.

	1952	1953	1954	1955
	1		3^{Hodge}	2, 4 ^{Hodge}
1956	1957	1958	1959	1960
5	6 7	8 9	24 25 Hirzebruch	26 ^{To}
1961	1962	1963	1964	1965
27 28 29	31 32 33	56	39 ^{Sh} 40 57	41 58
30 34 35	36 37 38	Singer	Bott	41 50
Hirzebruch	Hirzebruch	Singer	Dott	
1966	1967	1968	1969	1970
10 42 ^A 43	45 59	46 63 64 65 66	11 47 ^{Ta} 48	50 53 72
44 60 61	62 84	Bott Singer Segal	49 69 70 71	73 74 85 ^G
Bott	Bott		Segal Singer	Hirzebruch Bott
1971	1972	1973	1974	1975
51 67	52 ^{Du}	77 79 ^P	12 54 Sm 78	81 ^P 82 ^P
68 75		80 ^P 86 ^G		87 88
Segal Singer		Bott Singer		Singer
1976	1977	1978	1979	1980
13 14 15	16 55 90 ^{Sch}	17 // 96 ^{DM}	99	100 103
	91* 94 ^H 95 ^W	97 ^H 98 102 ^J		
Singer	Singer	Hitchin Singer		
1981	1982	1983	1984 19 20 21 22a	1985
101 104 106	18 92 ^D	93 ^D 107	109 110 112 117	23 // 115 116
	105 111 113 114	108^{Pr}	119 120 121	122 123 124
Bott	Singer Bott	Singer	Bott Singer	Hitchin
1986	1987	1988	1989	1990
22b 128	118 127	126 131 134 145	132 138 141 ^M	129 130 135
		Hitchin	Segal	136 137 139Je
1991	1992	1993	1994	1995
140		142 ^M 147 148	143 149 <u>154</u>	144 150
1996	1997	1998	1999	2000
133 <i>152</i>		146 151 155 156	157	159 161
2001	2002	2003	2004 125 162	
<i>153</i> 163 164	158 160 166 ^{Su}	167 ^{Su} 171 ^{Be}	172 ^{Ho} 173	
165 169 ^{MV}	168 ^{Bi} 170 ^{Wi}		Segal	

A Adams \cdot Be Berndt \cdot Bi Bielawski \cdot D Donnelly \cdot Du Dupont \cdot DM Drinfeld-Manin J Jones \cdot Je Jeffrey \cdot G Gårding \cdot H Hitchin \cdot Ho Hopkins \cdot M Manton \cdot MV Maldacena-Vafa \cdot P Patodi \cdot P Pressley \cdot R Rees \cdot Sch Schmid \cdot Sh Shapiro \cdot Sm Smith Su Sutcliffe \cdot Ta Tall \cdot To Todd \cdot W Ward \cdot Wi Witten \cdot * unpublished

OUTSTANDING WORKS WITH MAIN COLLABORATORS

HIRZEBRUCE

9 papers, making about 170 pages. Concentrated in the period 1959-1962.

- 24 Riemann-Roch theorems for differentiable manifolds.
- 25 Quelques théorèmes de non-plongement pour les variétés differentiables.
- 27 Bott periodicity and the parallelizability of the spheres.
- 28 Vector bundles and homogeneous spaces.
- 36 Analytic cycles on complex manifolds.
- 37 The Riemann-Roch theorem for analytic embeddings.

SINGER

The most sustained collaboration, from 1963 to 1984; 15 papers, making about 345 pages; for 7 of these (about 175 pages) he is the only coauthor.

- 56 The index of elliptic operators on compact manifolds [cf. poster 2]
- 64, 66, 67, 68 The index of elliptic operators [~ 135 pages; cf. Segal 65 below]
- 81, 82, 83 (w. Patodi) Spectral asymmetry and Riemannian geometry [~ 145]
- 92 (w. Donelly) Geometry and analysis of Shimizu L-functions.
- 93 (w. Donelly) Eta invariants, signature defects of cusps and values of L-functions
- 120 Dirac operators coupled to vector potentials.

BOTT

The most productive collaboration, sustained in the period 1964-1983; 12 papers, making about 475 pages; for 8 of these (about 255 pages) he is the only coauthor.

- 39 (w. Shapiro) Clifford modules.
- 40 On the periodicity theorem for complex vector bundles.
- 57 The index problem for manifolds with boundary
- 62, 63 A Lefschetz fixed-point formula for elliptic complexes [~ 75 pages]
- 79 (w. Patodi) On the heat equation and the index theorem.
- 85, 85 (w. Gårding) Lacunas for hyperbolic differential operators with constant coefficients [~ 140 pages]
- 105 The Yang-Mills equations over Riemann surfaces [~ 90 pages]
- 109 The moment map and equivariant cohomology.

SEGAL

4 papers, scattered from 1968 to 2004, making about 100 pages.

- 49 Equivariant K-theory and completion.
- 65 The index of elliptic operators [cf. Singer 64, 66, 67, 68 above]
- 173 Twisted K-theory

HITCHIN

6 papers, making about 340 pages; for 3 of these (about 150 pages) he is the only coauthor. Hitchin is the latest main collaboration, 1977-1988.

96 (w. Drinfeld and Manin) Construction of instantons.

[The celebrated ATIYAH-HITCHIN-DRINFELD-MANIN construction!]
97 (w. Singer) Self-duality in four dimensional Riemannian geometry.
126 Geometry and dynamics of magnetic monopoles [~ 130 pages]

Collaboration with Raoul [1926-2005] has been one of the great personal and mathematical pleasures of my life. Our work together undoubtedly reflects, and in turn enhances, our long friendship, emphasizing that mathematics is still a human activity, and has not yet been reduced to a computer program.

[MFA, A Personal History]

OTHER COLLABORATIONS

HODGE: 4, Integrals of the second kind on an algebraic variety.

TODD: 26, On complex Stiefel manifolds.

ADAMS: 42, K-theory and the Hopf invariant.

TALL: 47, Group representations, λ -rings and the *J*-homomorphism.

DUPONT: 52, Vector fields with finite singularities.

SMITH: 54, Compact Lie groups and the stable homotopy of spheres.

REES: 76, Vector bundles on projective 3-space.

SCHMID: 90, A geometric construction of the discrete series for ss Lie groups.

WARD: 95, Instantons and algebraic geometry.

JONES: 102, Topological aspects of Yang-Mills theory.

PRESSLEY: 108, Convexity and loop groups.

JEFFREY: 139, Topological Lagrangians and cohomology.

MANTON: 142 Geometry and kinematics of two skyrmions.

SUTCLIFFE: 166, The geometry of point particles.

167, Polyhedra in Physics.

BIELAWSKI: 168, Nahm's equations, configuration spaces and flag manifolds.

MALDACENA & VAFA: 169, An M-theory flop as a large N duality.

WITTEN: 170, M-theory dynamics on a manifold of G_2 -holonomy. [106 p.]

BERNDT: 171, Projective planes, Severi varieties and spheres. [28 p.]

HOPKINS: 172, A variant of K-Theory: K_{\pm} . [10 p.]

ATIYAH'S STUDENTS

Professor ATIYAH has had about 50 students. To name a few: SIMON DONALDSON, NIGEL HITCHIN, FRANCIS KIRWAN, PETER KRONHEIMER, GEORGE LUSZTIG, GRAEME SEGAL, SIMON DONALDSON was awarded the Fields medal in 1986 (Berkeley ICM).

CURRENT RESEARCH

MICHAEL ATIYAH is fully active in research and many other commitments. Currently, for example, he is cooperating with the distinguished neurophysilogist S. Zeki in studies of the human brain, particularly when it carries out mathematical tasks. He also keeps writing general essays on the nature of mathematics and its relation to science in general, and fundamental physics in particular.

Sources for posters 6 and 7

[1] M. F. ATIYAH: Collected Works. Oxford Science Publications, Clarendon Press, Oxford, 1988 (Volumes 1-5) and 2004 (Volume 6).